



# A Fixed Viewpoint Approach for Dense Reconstruction of Transparent Objects

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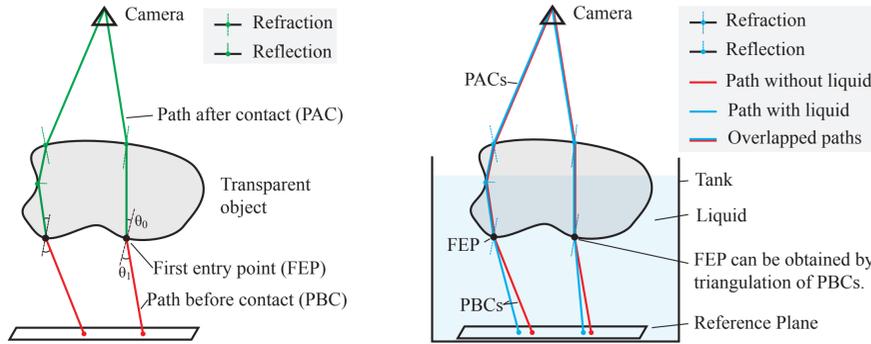
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## Problem Definition & Contribution

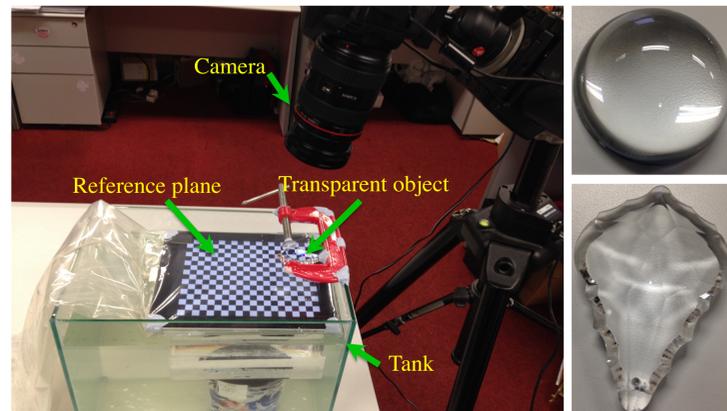
We are addressing the problem of dense reconstruction of transparent objects from a fixed viewpoint. In particular, we present a simple setup that allows us alter the incident light paths before light rays enter the object, and develop a method for recovering the surface by ray triangulation.



Compared with existing approaches, our proposed method has the following benefits:

- It does not assume any parametric form for the shape of a transparent object.
- It can handle a transparent object with a complex structure, with an unknown and even inhomogeneous refractive index.
- It considers only the incident light paths before light rays enter a transparent object, and makes no assumption on the exact number of refractions and reflections taken place as light travels through the object.
- The proposed setup is simple and inexpensive.

## Setup

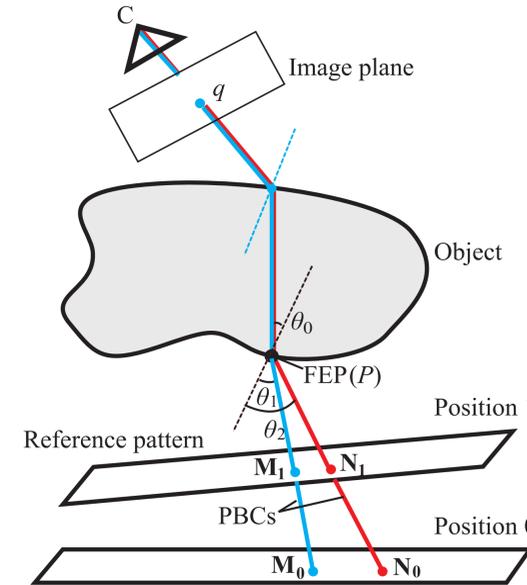


## Dense Refraction Correspondences

We employ an iPad as a reference plane and capture an image sequence of a white line sweeping horizontally and then vertically on a black background on the iPad screen. For each image point, its correspondence on the reference plane can be established by identifying the image frame in which its intensity attains a peak value. Knowing the correspondences on two distinct reference plane positions allows the recovery of the PBC for that image point.

## FEPs Reconstruction

Consider an image point  $q$  on the transparent object. Suppose  $M_0$  and  $M_1$  denote its correspondences on the reference plane under position 0 and position 1 with liquid in the tank, respectively. Similarly, let  $N_0$  and  $N_1$  denote its correspondences without liquid in the tank. We can construct two PBCs for  $q$ . The FEP can then be recovered as the point of intersection between the two PBCs. In practice, we seek  $M_c$  and  $N_c$ , respectively, on these two PBCs such that their distance is minimum among all the points on these two PBCs. We take the mid-point between  $M_c$  and  $N_c$  as the FEP for  $q$ .



## Surface Normal Recovery

Let  $\Delta\theta = \cos^{-1}(\mathbf{U} \cdot \mathbf{V})$  denote the angle between the two PCBs, where  $\mathbf{U}$  and  $\mathbf{V}$  are unit vectors being parallel to  $M_1M_0$  and  $N_1N_0$ , respectively. With known refractive indices  $\lambda_1$  and  $\lambda_2$  for the liquid and air, respectively, the incident angle  $\theta_1$  can be recovered by

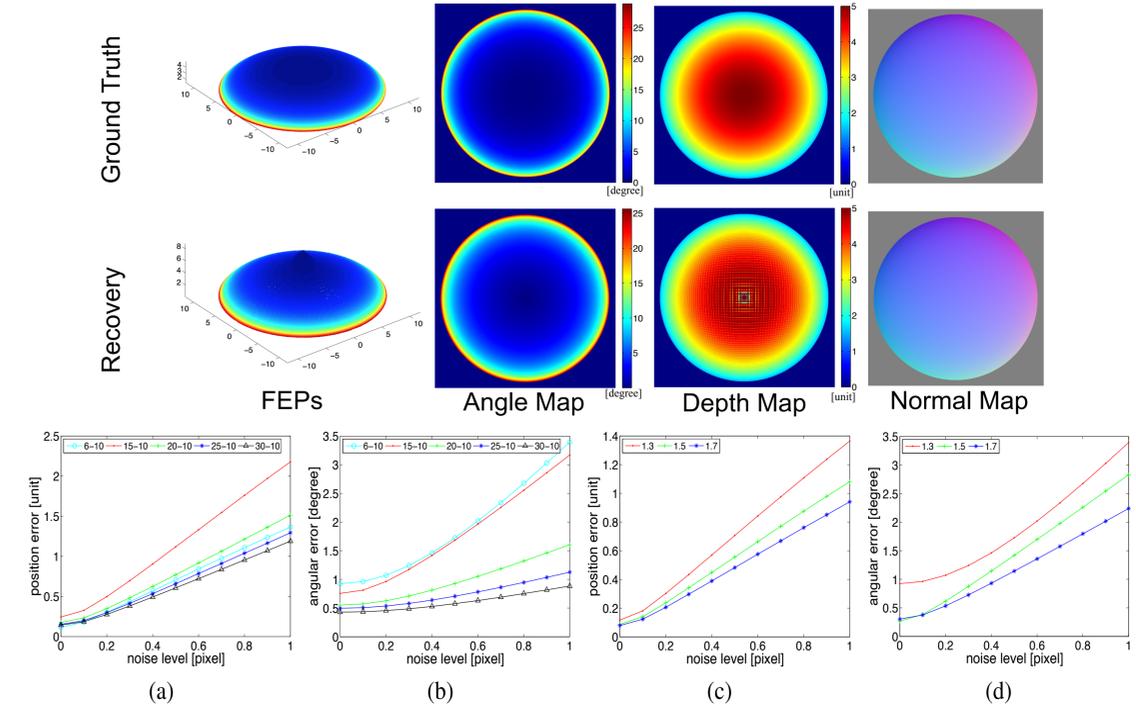
$$\theta_1 = \tan^{-1}((\lambda_2 \sin \Delta\theta) / (\lambda_1 - \lambda_2 \cos \Delta\theta))$$

The surface normal  $\mathbf{n}_p$  at  $P$  is then given by

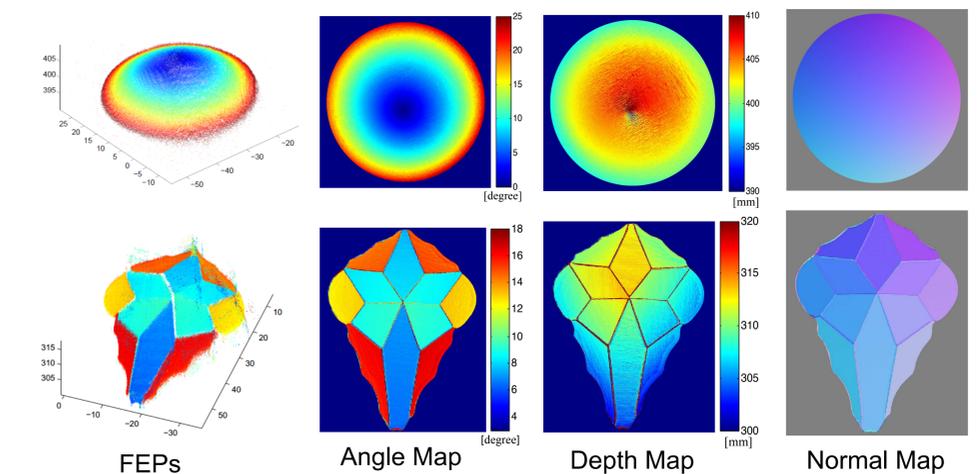
$$\mathbf{n}_p = \mathbf{R}(\theta_1, \mathbf{V} \times \mathbf{U})\mathbf{U}$$

where  $\mathbf{R}(\theta, \mathbf{a})$  denotes a Rodrigues rotation matrix for rotating about the axis  $\mathbf{a}$  by angle  $\theta$ .

## Experimental Results: Synthetic Data



## Experimental Results: Real Data



	Mean FEPs error (mm)	Mean normal error (degree)
hemisphere	0.59	6.97
ornament	0.73	7.34

